Principles and model for Risk evaluation (second wave)

Life Product Quantitative Evaluation

## Principles and model for Risk evaluation (second wave)

1. Where were we?
2. Profit testing of a new product
3. Risk Adjusted Capital: a simple and "practical" example

Where were we?: Methodology for Risk capital


$$
\begin{aligned}
& { }^{J} \text { RAC }=A C-{ }^{J} A C=(M V A-F V L)-\left({ }^{J} M V A-{ }^{J} F V L\right)
\end{aligned}
$$

$$
\begin{aligned}
& \text { ITechnical Component }
\end{aligned}
$$

$$
\begin{aligned}
& \text { I ( } \left.\mathrm{MVA}_{\text {отн }}-\mathrm{FVL}_{\text {отн }}\right)-\left(\mathrm{J}^{\mathrm{MVA}} \mathrm{OTH}-{ }^{\mathrm{J}} \mathrm{FV} \mathrm{~L}_{\text {отн }}\right) \\
& { }^{J} \text { RAC }_{\text {OTH }}=\text { ANAV }-{ }^{J} \text { ANAV } \\
& \text { Not Technical Component }
\end{aligned}
$$

## Where were we?: "Fair Value of Liabilities"

## Perché uno scenario non basta?

Uno scenario non è in grado di catturare i costi delle garanzie dei prodotti.

## Passo da 1 a 1.000 scenari:

La valutazione va ripetuta per tutti gli scenarie il valore finale sarà pari alla media dei valori ottenuti nei 1.000 scenari.

RISERVA LOCAL GAAP: è calcolata in un unico scenario:
$\xrightarrow[\text { PASSIVI }]{\text { ATTIVI }} \boldsymbol{\beta}$
$E^{\prime}$ il valore atteso dei cash flow nello scenario di $1^{\circ}$ ordine (ipotesi prudenti)

RISERVA A FAIR VALUE: la valutazione va ripetuta nei 1.000 scenari


La riserva è la media dei valori ottenuti nei 1.000 scenari con ipotesi best estimate:

$$
\frac{\sum_{j=1}^{1000}\left(\sum_{i=1}^{n} \text { Net Cash Flow }{ }^{20} \text { ordine } \times d_{i}\right)}{1000}
$$

```
PUNTI DI ATTENZIONE
Gli scenari stocastici devono catturare la diversa rischiosità degli attivi(bond governativi, corporate, azioni..)
Il rendimento medio nei 1.000 scenariè lo stesso per tutte gli attivi, ma più gli attivi sono rischiosi, maggiore è
la volatilità del loro rendimento (SCENARIDITIPO RISKNEUTRAL).
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## Risk Adjusted Capital: a simple and "practical" example

1. calcolare il valore di mercato delle riserve e degli attivi a data di valutazione:

2. sulla base del metodo di calibrazione dello stress calcolare la variazione del valore di mercato delle azioni: ad esempio la perdita è pari a 50 (150*33\%).
3. ricalcolare il valore delle riserve dove gli attivi in tutti i 1.000 scenari hanno un valore ridotto (-50). Le rivalutazioni delle prestazioni vengono diminuite in rispetto alle regole contrattuali

4. il requisito di capitale non è pari a $\mathbf{5 0}$ euro (come per esempio accade nel ramo danni) ma a 10 euro (50-40), retrocedendo l'80\% delle perdite gli assicurati.

L' aliquota di retrocessione agli assicurati risulta funzione dei rendimenti previsti e dei livelli di garanzia prestati.

| Capitale per rischio Equity: |  |  |
| :--- | ---: | :---: |
| Perdita attivi | 50 |  |
| Requisito pre assorbimento | 50 |  |
| Riduzione riserve: | -40 |  |
| Requisito post assorbimento | 10 |  |

## Methodology for Risk capital: Market Risk (1/3)

## Technical Component:

Case A: Unit Linked Portfolio w/o Guarantee


Change in Market Value $=50$
Change in Liabilities $=47$
RAC = AC - ACequity $=50-47=3$
Liability absorption $=$ change in liabilities $/$ change in assets $=47 / 50=95 \%$

- In a unit linked contract the market risk is in charge of the insured;
- the asset stress produced only a "proportional reduction" of the expected profits (total MVAssets $=-8 \%->$ AC -8\%)


## Methodology for Risk capital: Market Risk (2/3)

## Technical Component:

Case B: Term Assurance


Change in Market Value $=50$
Change in Liabilities $=0$
RAC $=A C-A C$ equity $=50$
Liability absorption = change in liabilities $/$ change in assets $=0 / 50=0 \%$

- In a term the market risk is in charge of the insurer
- the asset stress doesn't affect the liabilities, therefore all the stress produces a PVFP reduction


## Methodology for Risk capital: Market Risk (3/3)

## Technical Component:

Case C: Product with guarantee and Profit Sharing (80\%)


Change in Market value of Assets $=150 * 33 \%=50$
Change in FVL = 750-710=40
Change in AC = 250-240=10
Liability absorption =10/40=80\%
The loss is shared: $20 \% \mathrm{SH}, 80 \% \mathrm{PH}$

- In a product with profit sharing, both proifts and losses are shared; the \% of sharing is a function of the portfolio structure and the level of the stress
- In general we can notice an absence of linearity among the loss sharing partecipation and the increase of the stress level


## Life Products Quantitative Evaluation

1. Methodological framework
2. Profit testing of a new product
3. Measuring Profitability
4. Measuring capital absorption and remuneration
5. Profit breakdown
6. RAC calculated at individual product level
7. Sensitivities

## New Business Value: Definition

New Business Value = present value, at issue date, of future industrial profits (after taxes and reinsurance) expected to emerge from all contracts issued during the last year, taking into account the cost of holding the required capital

> Traditional valuation
> NBV = PVFP - CoC
> - PVFP $=\Sigma_{t} \frac{U_{t}}{(1+r)^{t}}$
> $U_{t}=$ industrial profit (after tax and reins)
> $r=$ discount rate
> - CoC $=\Sigma_{t} \frac{C_{t-1} *\left[r-i^{*}(1-\operatorname{tax})\right]}{(1+r)^{t}}$
> $C_{t-1}=$ capital
> $i=$ return on assets backing the capital
> $r=$ discount rate
$\mathrm{NBV}=\Sigma_{\mathrm{I}_{\mathrm{t}}} \frac{\mathrm{K}_{\mathrm{t}}}{(1+\mathrm{r})^{t}}$
Present value of distributable profits
$\mathrm{K}_{\mathrm{t}}=$ industrial + patrimonial profits (net of tax)+ yearly variations of the solvency margin

## Market consistent valuation <br> NBV = CE PVFP - TV of FG\&O - CoC - Allow. for NHR

- CE PVFP = Certainty Equivalent PVFP = the present value of future after tax and after reins. industrial profits calculated using the certaintyequivalent approach
- TV of FG\&O = Time Value of financial guarantees \& options = allowance for the potential impact on future industrial profits of all relevant financial guarantees and options =
= CE PVFP - mean of stochastic PVFPs
- $\mathbf{C o C}=$ Frictional costs of Required Capital $=$ represented by taxation and investment expenses on assets backing the required capital
- Allowance for NHR = allowance for non hedgeable risks = explicit allowance for residual non hedgeable risks not already allowed for in the PVFP and the TV


## New Business Value: Different Approaches

## Marginal

NBV = difference between portfolio value and value of old business

## PROS

- It takes into consideration the cross subsidies among old business and new business
- Properly measures the value creation in the year caused by the new production


## CONS

- It is complex
- It requires selection of assets backing old business; different selections may cause "artificial" NBV
- Due to one-off effects it is not appropriate to evaluate the Goodwill (NBV *multiple)


## Stand Alone

NBV calculated in isolation with its own assets, even if it insists on an open fund

## PROS

- New money investment rates are used and hence the NBV is valued in current market conditions environment
- Comparability: the same product produces the same value independenlty on the company that is selling it


## CONS

- It does not capture the effects deriving from the fact that the business is sold within a going concern;
- It does not reflect the way the business is actually managed (e.g. a perfect AL matching may be assumed, even if not applied in reality).


## Proportional

NBV is part of the existing business

## PROS

- Simpler and understandable practical implementation
- The attribution of gains and losses from in force business to the new production reflects the way business is managed


## CONS

- The attribution of gains and losses to new business may bring to their double counting
$>$ The methodology for the profit testing should be designed to be:
- applied at any valuation date through the year, whenever there is a new product launched by the Company
- consistent with the methodology applied by the Company for the Embedded Value and for the required capital calculations
$>$ The evaluation of the impact of the Time Value of Options and Guarantees require time consuming stochastic calculations
$>$ On the other hand, exporting these impacts from already available company new business value calculation works if and only if the new product launched is similar in terms of guaranteed rates, contracts durations and other relevant features to the new business already evaluated
$>$ To allow for consistent exportation: new business value granularity i.e. calculation of the time value of the part of new business that is similar to the new tariff


New Business Margin (NBM) = NBV / APE = New Business Value/Annual Premium Equivalent (Regular premium+single premium/10)
> It is a multi-period profitability indicator
> Strength: widely used and easy to understand
> Weaknesses: normalized assumption of 10 years of duration for single premiums

## NBV/P.V. Premiums = New Business Value/Present Value of Future Premiums

> Expresses the profitability as a percentage of the products yearly turnover
> Strength: solves the problem of the normalization used in the NBM, representing the effective duration of the contract

## NBV/P. V. Reserves = New Business Value/Present Value of Future Premiums

> Expresses the profitability as a percentage of assets under management of the company related to the product under analysis
$>$ Strength: is a good measure of the annual profitability in terms of managed assets
$>$ Weakness: meaningless for products where the mathematical reserve is a very small amount (e.g. Pure risk products)

## Profitability ratios based on volumes: which indicator should we look at?

The 3 ratios give different indications!

|  | Product 1 | Product 2 | Product 3 |
| :--- | ---: | ---: | ---: |
| NBV/PVR | $0,96 \%$ | $0,66 \%$ | $0,45 \%$ |
| NBV/PVP | $4,03 \%$ | $4,13 \%$ | $3,68 \%$ |
| NBM | $33,48 \%$ | $44,62 \%$ | $46,21 \%$ |
| APE | 1.000 | 1.000 | 1.000 |
| Term | 10 | 15 | 20 |
| Fee | $0,85 \%$ | $0,80 \%$ | $0,70 \%$ |

## Assume

- Recurrent premium financial product;
- $2 \%$ Cliquet guarantee;
- $10 \%$ loading on premium;
- $5 \%$ of sum of premium commission;
- $0,2 \%$ of reserves of financial/management expenses,
- $3 \%$ risk capital
- $35 \%$ tax
- 3\% yearly surrender rates
- death according to SIM 1992
- Investment returns among 2,5\% and 3,5\%

PVR: Present Value of Reserves PVP: Present Value of Premiums

- NBM: the less profitable is Product 1
- the denominator is the same for the 3 products (equal to 1000) and hence increasing the term brings to higher NBV that is reported to the same amount leading to a higher value of the ratio
- the effect of the annual loss of the fee ( $0.15 \%$ between Products 1 and 3 ) is lower of the effect of gaining it for a longer time
- NBV/PVP: the less profitable is Product 3
- the denominator varies i.e. increases with the term; in Product 3 the NBV (the same as in the NBM) is divided by a higher amount
- NBV/PVR: the less profitable is Product 3 but the most profitable is Product 1
- this indicator rewards the product with higher management fee


## Profitability ratios based on volume: impact of direct and indirect expenses ${ }_{16}$

A more detailed analysis of the profitability can be performed by calculationg the mentioned profitability ratios by changing the numerator with the puprose of isolating the impact of:

Commissions,
 underwriting, training for the sales force, policy conditions and illustrative Indirect expenses: Other expenses (e.g. personnel costs) material for clients ...


Profitability before direct and indirect expenses
Expected to be always positive

| Profitability before indirect, after direct expenses | $\longrightarrow$Expected to be positive meaning that the <br> product is at least able to support <br> commissions i.e. the direct expenses |
| :--- | :--- |
| Profitability before expense overrun, |  |
| after direct and indirect |  | | For start-up companies that are temporarily in a |
| :--- |


|  | After direct <br> and <br> indirect <br> exp. | Before exp. <br> overrun after <br>  <br> indirect exp. | Before <br> indirect <br> after direct <br> exp. | Before <br> direct and <br> indirect <br> exp. |
| :--- | ---: | ---: | ---: | ---: |
| 1. Net Profitability ratios | $51.76 \%$ | $51.76 \%$ | $132.50 \%$ | $172.41 \%$ |
| NBV/APE | $5.77 \%$ | $5.77 \%$ | $14.76 \%$ | $19.21 \%$ |
| NBV/P.V. Premiums | $\mathbf{0 . 7 6 \%}$ | $0.76 \%$ | $1.94 \%$ | $2.53 \%$ |
| NBV/P.V. Technical Resenes |  |  |  |  |


|  |  | After direct <br> and <br> indirect <br> exp. | Before exp. <br> overrun after <br>  <br> indirect exp. | Before <br> indirect <br> after direct <br> exp. |
| :--- | ---: | ---: | ---: | ---: |
| 1. Net Profitability ratios | Before <br> direct and <br> indirect <br> exp. |  |  |  |
| NBV/APE | $-9.32 \%$ | $-9.32 \%$ | $4.71 \%$ | $15.29 \%$ |
| NBV/P.V. Premiums | $-0.93 \%$ | $-0.93 \%$ | $0.4 \%$ | $1.53 \%$ |
| NBV/P.V. Technical Reserves | $-0.17 \%$ | $-0.17 \%$ | $0.09 \%$ | $0.28 \%$ |

Product that supports direct expenses but not the indirect that can anyway be acceptable becuase absorbs expenses of other products

|  | After direct <br> and <br> indirect <br> exp. | Before exp. <br> overrun after <br>  <br> indirect exp. | Before <br> indirect <br> after direct <br> exp. | Before <br> direct and <br> indirect <br> exp. |
| :--- | ---: | ---: | ---: | ---: |
| 1. Net Profitability ratios | $12.60 \%$ | $17.17 \%$ | $43.26 \%$ | $59.20 \%$ |
| NBV/APE | $2.06 \%$ | $2.01 \%$ | $7.08 \%$ | $9.69 \%$ |
| NBV/P.V. Premiums | $0.36 \%$ | $0.50 \%$ | $1.25 \%$ | $1.71 \%$ |
| NBV/P.V. Technical Reserves |  |  |  |  |

Example of start-up company with expense overrun

## Return on Risk Adjusted Capital (RoRAC) = (Industrial profit of the year + Return on Risk Capital)/ Risk Capital

> No prospective view (as in EV or NBV), but only reference to the result of the year: compares the reuslt of the year with the capital necessary to support the business of the year

## Average RoRAC $=\frac{\text { PV Return on Risk Capital }+ \text { PV Industrial Profit }}{\text { PV Risk Capital }}$

> It is the weighted average of the annual returns with weights equal to the discount factors
> Catches the perspective view on the run-off of the generation of the new business/new product considering the RAC totally allocated to the new business/product and the total profit produced by it over the whole projection period

## NBV/P.V. Required Capital

> It is a profitability indicator that however compares the profitability to the capital necessary to support it
> Similar to the Average RoRAC

## Internal Rate of Return = the discount rate that makes the net present value of distributable profits equal to zero

| STRENGHTS | WEAKNESSES |
| :--- | :--- |
| Widely used, easy to calculate and to be understood by the <br> management because it is similar to the concept of RoE <br> (Return on Equity) | May not exist (e.g. where there is no intial investment) |
| Allows comparison among dissimilar investments | In case of low initial strain, it can be extremely high and <br> difficult to interpret |
| Helps to understand the remuneration of the invested <br> capital from a shareholder perspective | May have multiple values (e.g. in case of positive cash <br> flows followed by negative ones and then agian by <br> positive ones) |
|  | Assumes reinvestment of interim cash flows in projects <br> with equal rates of return |

> Being internal, it refers to monetary items and has to be "judged" in respect to local currency interest rates (Ex: 10-year local government bond + a spread)

## Comparing the IRR with the RoRAC

> The Average RoRAC always exists
> If the discount rate used in the average RoRAC is equal to the IRR, the Average RoRAC is equal to the IRR

## Remuneration of the employed capital: IRR

> Can be caluclated on industrial and on distributable profits

## Further analysis

## IRR on distributable profits

=
weighted average of
IRR on industrial profits and the IRR on the capital
necessary to support the business

## Interpretation:

$\checkmark$ the level of the IRR on distributable profits is closer to the IRR on industrial profits when the capital required to support the product/business is relatively low;
$\checkmark$ Increasing the required capital means moving the average towards the 4\%
$>$ Additional effect of taxes that can bring distortion in the average

| IRR on <br> distributa <br> ble profits <br> after tax | IRR on <br> Industrial <br> profits | IRR on <br> Required <br> Capital <br> before tax | IRR on <br> Distributable <br> Profits <br> before tax |
| ---: | ---: | ---: | ---: |
| $4.90 \%$ | $5.3 \%$ | $3.9 \%$ | $5.2 \%$ |

## Remuneration of the employed capital: Profit Signature

$>$ Besides the ratios/indicators that analyse the product in a perspective view though via comparisons of "present values", it is interesting and useful to have a look to the yearly profits to detect possible anomalous effects


- The typical Product profit profile is featured an initial loss, to be divided among the industrial strain due to commissions and the capital absorption, followed by a set of (hopefully!) positive profits

- Sharp drop of the distributable profit in year 26 ... ???
- Negative industrial and distributable losses in the final years of the contract ... ???


## New Business Strain = Sum of yearly losses divided by the first year premium

$>$ On industrial profits: highlights the impact on the P\&L of the initial investment in terms of commissions and other acquisition expenses
$>$ On distributable profits: measures also the negative effect of setting aside the required capital
From industrial to distributable profits: tax effect

## SOME CONSIDERATIONS

$>$ Regular premium contracts usually have higher NB strain than single premium contracts because of:

- the impact of the up-front commissions paid on regular premiums
- regular premiums are generally more remunerated than single premiums
$>$ Among regular premiums the NB strain varies due to:
- term of the contract
- the level and the way commissions are paid: how much is paid up-front and how much is the regular commission spread over the whole duration of the contract
$>$ The NB strain should be evaluated on "pure" cash flows because accounting practices such as DAC (Deferred Acquisition Costs) artificially alter the result of the first year
$>$ Measures that concretely decrease the NB strain:
- Zillmer reserves
- Profit sharing system in which the policyholder participates to all source of profits (the first year loss is shared between policyholder and shareholder)


## Pay-back period

## Modified pay-back period

= Period of time required to repay the sum of the original investment
= Period of time required to repay the sum of the original investment but in case of several changes of sign, the pay-back corresponds to the moment in which the cumulative positive inflows exceed the total outflows
> Can be calculated on industrial profits and on distributable profits
$>$ Should be based on pure cash flows


Example: Annuity product with losses in the last years


- Red dotted line: cumulated profits
- In the example, more than one payback period exists
- Green dotted line: cumulated positive results minus the sum of all negative results (modified payback period that is unique and only exists when the sum of profits is positive)
- Red dotted line: pay-back period in which final losses are not taken into account
- Green dotted line: final losses of the annuity are taken into account


## Remuneration of the employed capital

$>$ Similarly to what can be done for the IRR, these three indicators can be seen as the sum of:
$\checkmark$ Effect on industrial profits
$\checkmark$ Effect on the required capital
$\checkmark$ Effect on taxes
> Example on New Business Strain

| NB Strain on <br> distributable <br> after tax | of which <br> industrial <br> effect | of which <br> capital <br> effect | of which <br> tax <br> effect |
| ---: | :---: | :---: | :---: |
| $-\mathbf{2 8 . 5 \%}$ | $-36.3 \%$ | $-2.8 \%$ | $10.6 \%$ |

Positive effect of taxes due to the losses

## Pay-back Period towards Duration

> The pay-back should be "judged" together with the contract duration

- Example of a possible reference economic threshold: a combination of an absolute $\mathrm{n}^{\circ}$ of years and a parameter linked to the contract duration that captures the peculiarity of the product under analysis
$>$ The Profit Period = contract duration - payback period: period of the contract in which the company is expected to make profit
- Example: setting an economic threshold for the pay back period equal to $2 / 3$ of the contract duration means that the shareholder has to wait for $2 / 3$ of the duration to recover the investment, the remaining $1 / 3$ is to make profit
$>$ Products/Portfolios with long pay-back can be sustainable if:
$\checkmark$ the duration of the products is also long
$\checkmark$ the company can rely on a stable portfolio to avoid that the policyholder leaves the company before the capital employed is recovered


High persistency to be achieved via:
$\checkmark$ Claw-back mechanisms
$\checkmark$ Regular Commissions dependent on portfolio persistency $\checkmark$ Surrender penalties and fidelity/terminal bonuses

Gross profit breakdown in \% of PV Reserves

$>$ Gives indication on the equilibrium of the product among different sources of profits:

- What is the main source of profit of the product?
- Is it highly exposed on the financial side?
- Are the loadings sufficient to cover the expenses?


## Analysis of the product from the Policyholder's persepctive

## Policyholder's IRR

- Negative or very low IRR for the policyholder on saving products may arise potential reputational risk for the Insurance Company
- Problem of the emerging markets where there are cases in which the policyholder does not recover the money invested in the insurance contract even if he stays in the contract for many years




## RAC at product level

> In a Solvency II perspective, when a new product is launched, it shall be evaluated in terms of capital absorption and remuneration
> Estimate of the RAC at product level, possibly with simplified procedures that avoid fully stochastic calculations but too strong approximations (e.g. rescaling of the RAC calculated for the total new production or even worse that on the existing contracts) may be meaningless leading to totally misleading allocation of capital to the new product the company is going to launch

$>$ Solvency II is not only only quantitative time consuming and reporting but it is:

- an instrument to improve the risk management in the "real world"
- a better efficiency in the capital management


## Sensitivities

> Once having calculated the RAC at product level, is it still necessary to perform the sensitivities (it could be argued that "stresses" of the RAC and "sensitivities" are substantially the same concept ...)?
> The answer should be "yes": the "stresses" applied in the calculation of the RAC are aiming at evaluate the losses in extreme situations, the "sensitivities" are in a way "complementary" to them aiming at assuring that the product is overall in equilibrium in case of slight deviations from the base assumptions
> Examples of the usual sensitivities:

- Risk Free +/-1\%
- Maintenance/Financial Expenses: -10\%
- Lapse rates * $90 \%$
- Lapse rates * 110\%
- Mortality/Morbidity *95\%
> Besides, it may be useful to perform an additional sensitivity (or more than one):
- on the model point that provides the maximum level of $\qquad$
Product seen commissions to the sales force to make sure that it is sustainable also from the sales force perspective!


## NBV/P. V. (Commissions+Other Acquisition costs)

- the profit of the company per unit of currency necessary to acquire the new business, in terms of commissions paid to sales forces and other acquisition expenses


## V. FINALREMARKS

Generali on new life production


[^0](3) PSL cost of investment in life new business

Assicuratori Generali Group - Ifreestor Day 2010 - Investment Maragenent of Insuranoe Assets

## Q: What does Free Surplus mean at product level?

## A: Free Surplus = NBV - RAC

Q: When a new product is self financing?
A: When it does not require a capital injection:
> In Solvency 1: NEVER
> In Solvency 2: «could be» if the expected profits are considered as TIER 1 capital

## ORSA: New Products and Capital Absorption

$\Gamma$

90/10 with profit contract , 15 yrs contractual term: Yearly vs At Maturity Guarantee


## ORSA: New Products and Capital Absorption

90/10 with profit contract , 15 yrs contractual term: Yearly vs At Maturity Guarantee


## ORSA: New Products and Capital Absorption

$\Gamma$

Free Surplus Volatility: Yearly vs At Maturity Guarantee


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## Free Surplus Volatility: Yearly vs At Maturity Guarantee



## ORSA: New Products and Capital Absorption

90/10 with profit contract , 15 yrs contractual term: Single vs Annual Premium


## ORSA: New Products and Capital Absorption

90/10 with profit contract , 15 yrs contractual term: Single vs Annual Premium


## ORSA: New Products and Capital Absorption




[^0]:    (1) Required casilal due so new business production
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